Deep reinforcement learning in a time-continuous model

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Inspired by the recent success of deep learning [1], several models emerged trying to explain how the brain might realize plasticity rules reaching similar performances as deep learning [2, 3, 4, 5]. However, all of these models consider only supervised and unsupervised learning, where an external teacher is needed to produce an error signal that guides plasticity.

In this work, we introduce a model of reinforcement learning with the principle of Neuronal Least Action (R-NLA). We extend previous works on time-continuous error backpropagation in cortical microcircuits [4, 6] to achieve a biologically plausible model implementing deep reinforcement learning.

In R-NLA the neurosynaptic dynamics is derived from the energy function using the variational principle. In the resulting dynamics the phase-advanced firing of the neurons effectively undoes the network delay introduced by finite membrane time-constants. Errors are introduced to the network by nudging, and they are propagated to deeper layers via cortical microcircuits. Instead of having an explicit teacher, the output neurons, which represent the actions, form a soft winner-take-all network (Fig A). This winner-take-all structure evokes a nudging on the soma of the output neurons, which is subsequently backpropagated through the network. A reward prediction error $\delta = R - \langle R \rangle$ modulates the plasticity multiplicatively as a formally deduced global reward-specific neuromodulator [7]. By construction, the learning rule approximates the policy gradient of the mean expected reward.

We show, on a toy problem, that R-NLA can learn classification tasks in the reinforcement learning framework with similar performance as an equivalent deep reinforcement learning model (Fig B). Further, we show that it is robust against time delayed rewards, even if the reward-delay is not constant but randomly distributed (Fig C).

R-NLA constitutes a time-continuous implementation of biologically plausible deep reinforcement learning, robust to delayed reward. The self-teaching soft winner-take-all mechanism removes the necessity of an explicit teacher and the proposed learning rule solves the problem of synaptic consolidation. The model can be extended to an actor-critic model, where a second (deep) critic network learns the state-value function.

References

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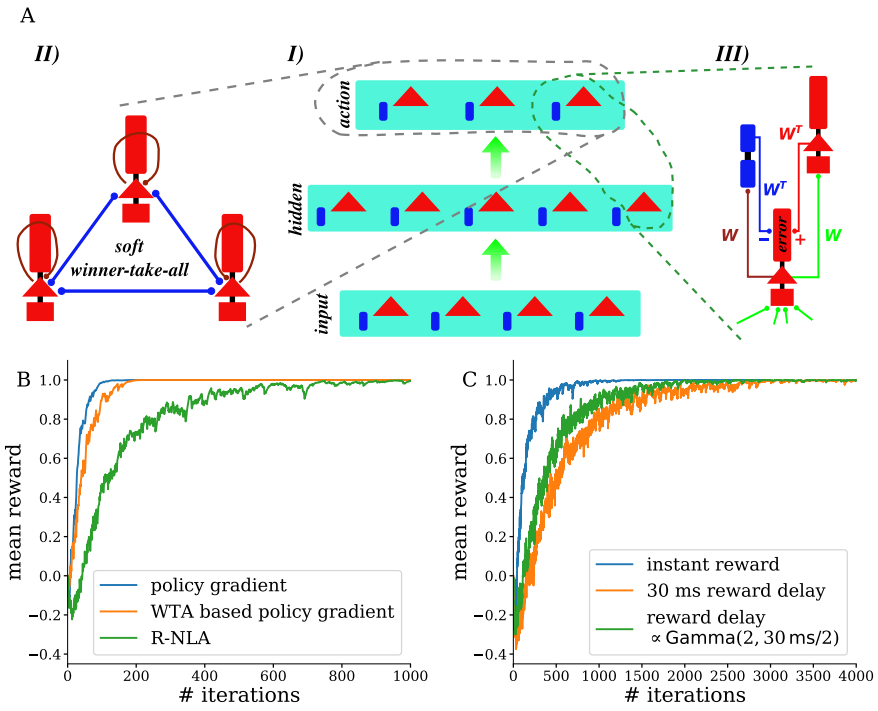

Figure 1: **A-I** Network schematics. **A-II** Soft winner-take-all network in the output layer. **A-III** Microcircuit for error backpropagation. **B** Comparison to classical reinforcement learning methods. **C** Robustness with respect to reward delays.

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