

Nonthermal fixed points and superfluid turbulence

Boris Nowak



S. Erne, M. Karl, M. Schmidt, J. Schole, D. Sexty, T. Gasenzer

Institut für Theoretische Physik
Ruprecht-Karls Universität Heidelberg

Philosophenweg 16 • 69120 Heidelberg • Germany

email: b.nowak@thphys.uni-heidelberg.de
www: www.thphys.uni-heidelberg.de/~gasenzer



Nonequilibrium Dynamics



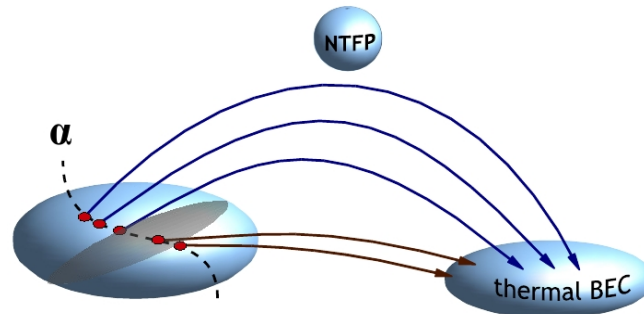
Initial state:
Far from equilibrium



Transient state:
e.g. Turbulence
(Nonthermal fixed point)



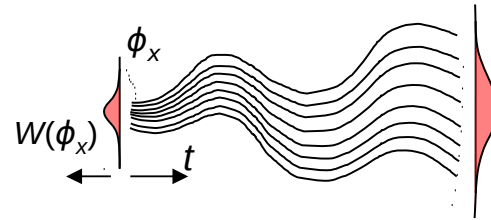
Final state:
Thermal equilibrium



Semi-classical simulations

Classical field equation for $\phi(\mathbf{x}, t)$:

$$i\partial_t\phi(\mathbf{x}, t) = \left[-\frac{\nabla^2}{2m} + g|\phi(\mathbf{x}, t)|^2 \right] \phi(\mathbf{x}, t)$$

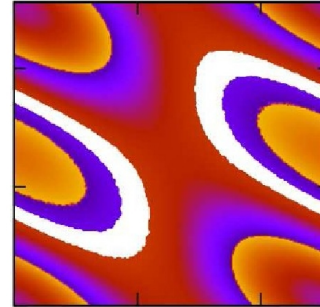
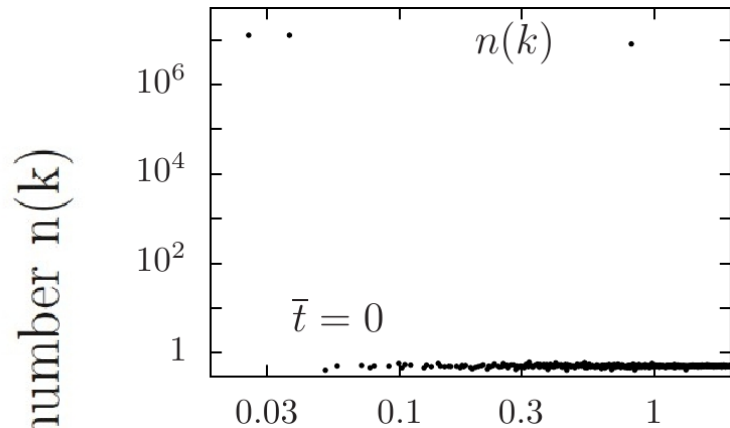


Observables: e. g. Momentum distribution

$$n(k) = \int d^{d-1}\Omega_k \langle \phi^*(\mathbf{k})\phi(\mathbf{k}) \rangle_{\text{ensemble}}$$



2D: Quench dynamics

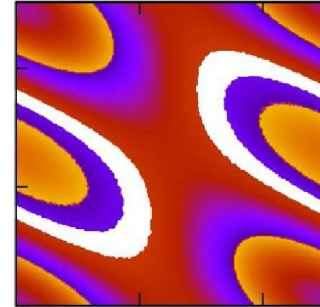
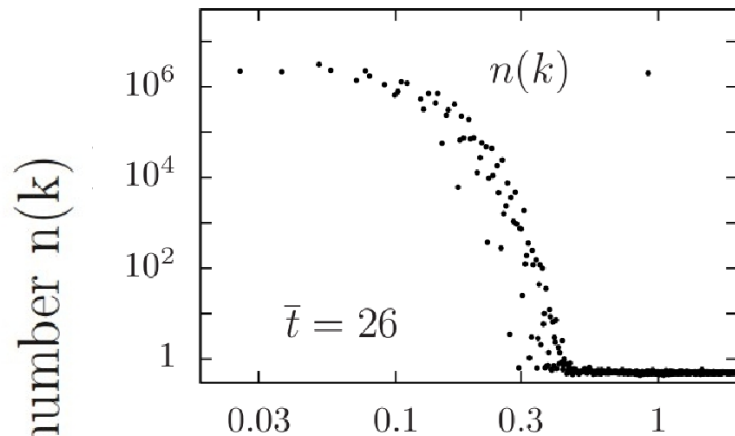


Radial momentum k

BN, D. Sexty, T. Gasenzer PRB 84(R) (2011), BN, J. Schole, D. Sexty, T. Gasenzer PRA 85 (2012)



2D: Quench dynamics

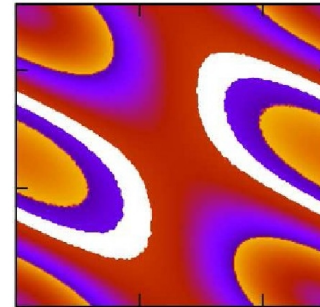
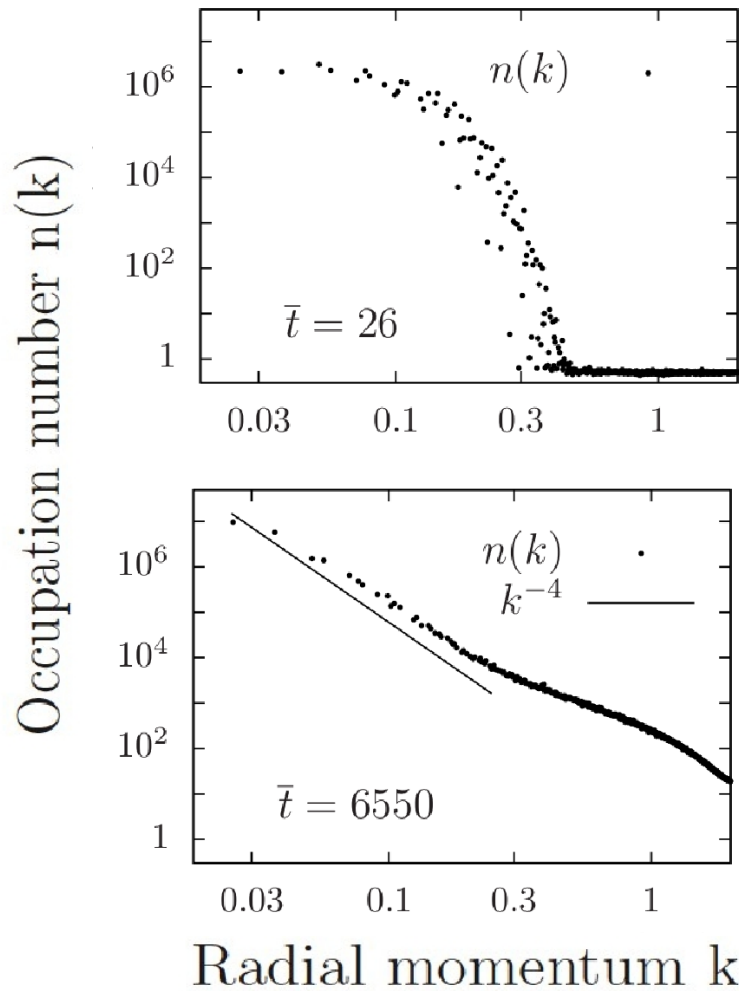


Radial momentum k

BN, D. Sexty, T. Gasenzer PRB 84(R) (2011), BN, J. Schole, D. Sexty, T. Gasenzer PRA 85 (2012)



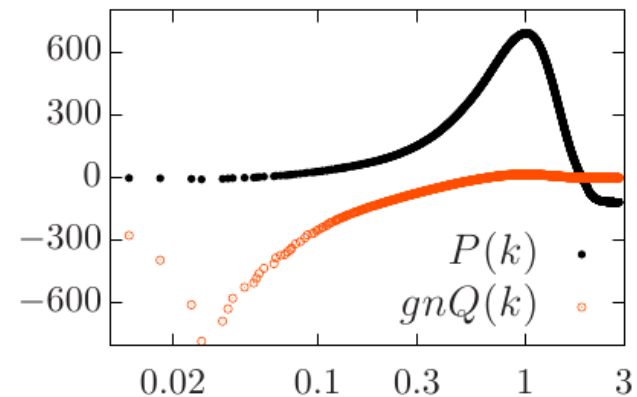
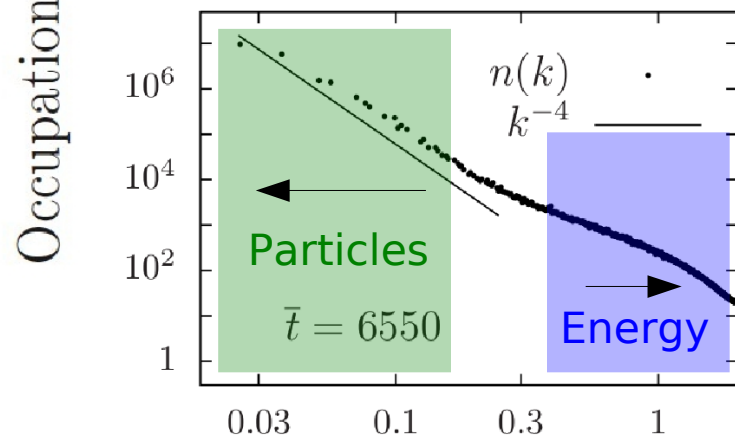
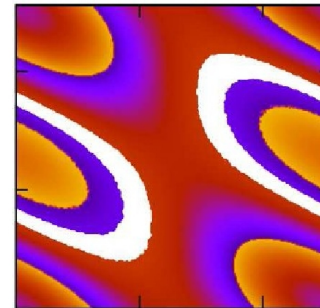
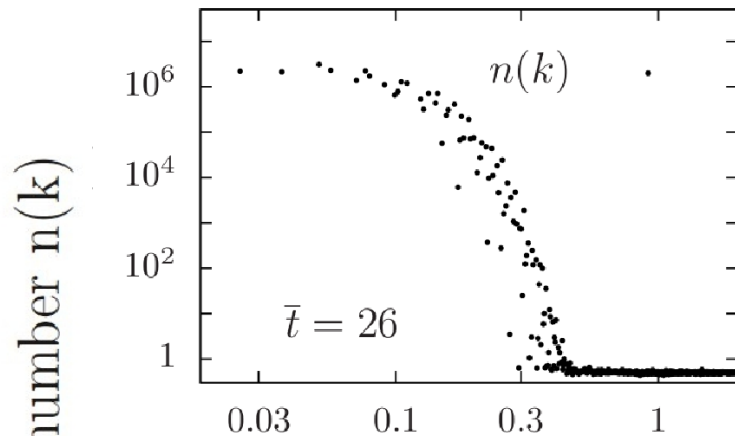
2D: Quench dynamics



BN, D. Sexty, T. Gasenzer PRB 84(R) (2011), BN, J. Schole, D. Sexty, T. Gasenzer PRA 85 (2012)



2D: Quench dynamics

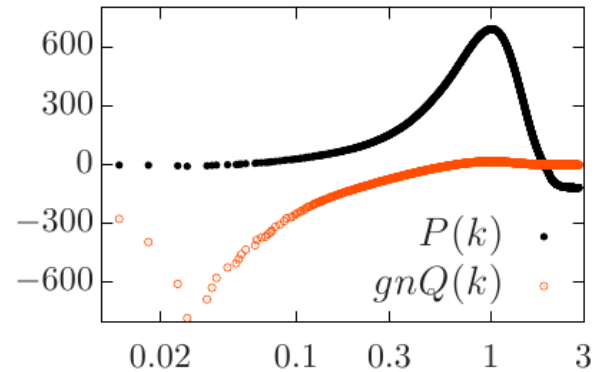
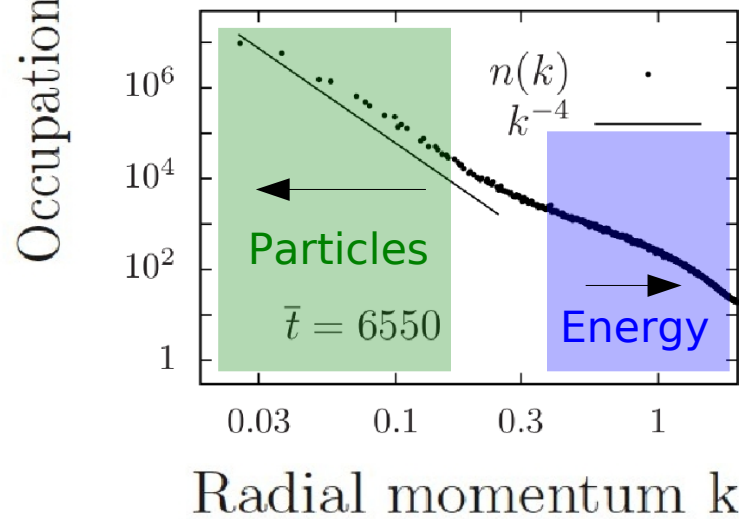
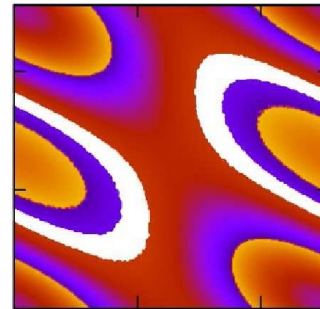
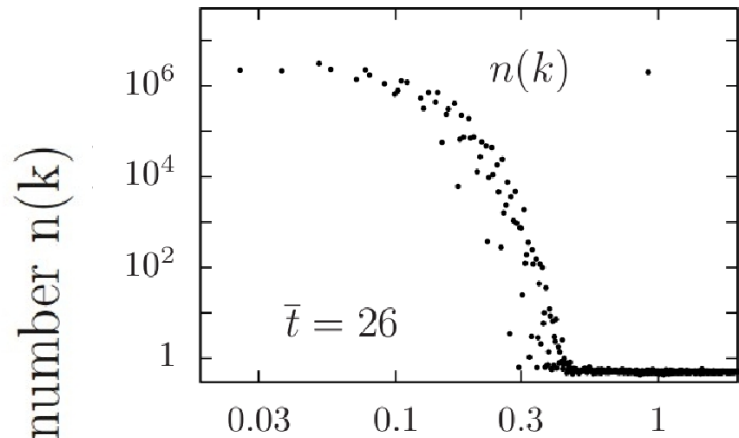


Radial momentum k

BN, D. Sexty, T. Gasenzer PRB 84(R) (2011), BN, J. Schole, D. Sexty, T. Gasenzer PRA 85 (2012)



2D: Quench dynamics



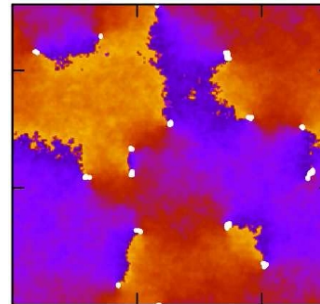
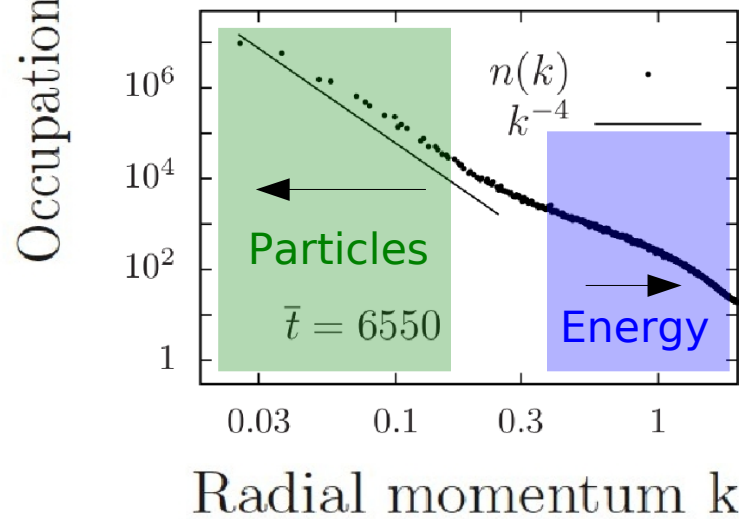
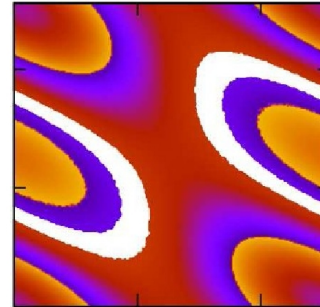
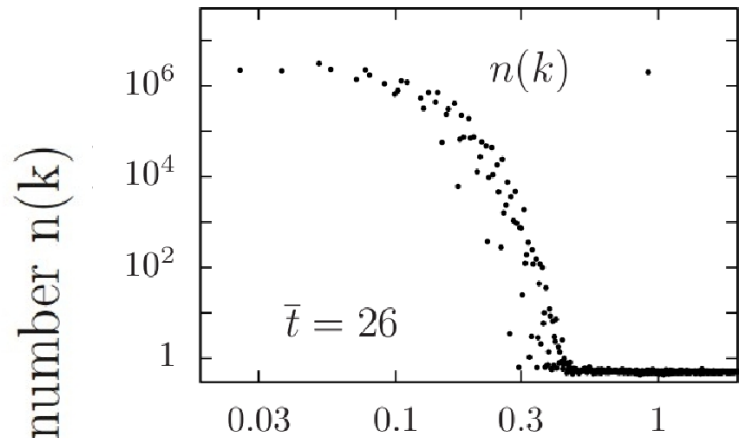
$$\text{X} \rightarrow \text{X} = \text{X} + \text{X}$$

J. Berges, A. Rothkopf, J. Schmidt PRL (2008)
 C. Scheppach, J. Berges, T. Gasenzer, PRA (2010)

BN, D. Sexty, T. Gasenzer PRB 84(R) (2011), BN, J. Schole, D. Sexty, T. Gasenzer PRA 85 (2012)



2D: Quench dynamics



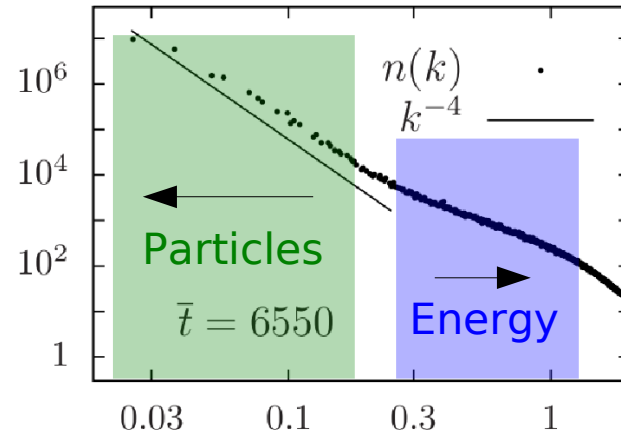
$n_k \sim k^{-4}$

$E_k \sim k^{-1}$

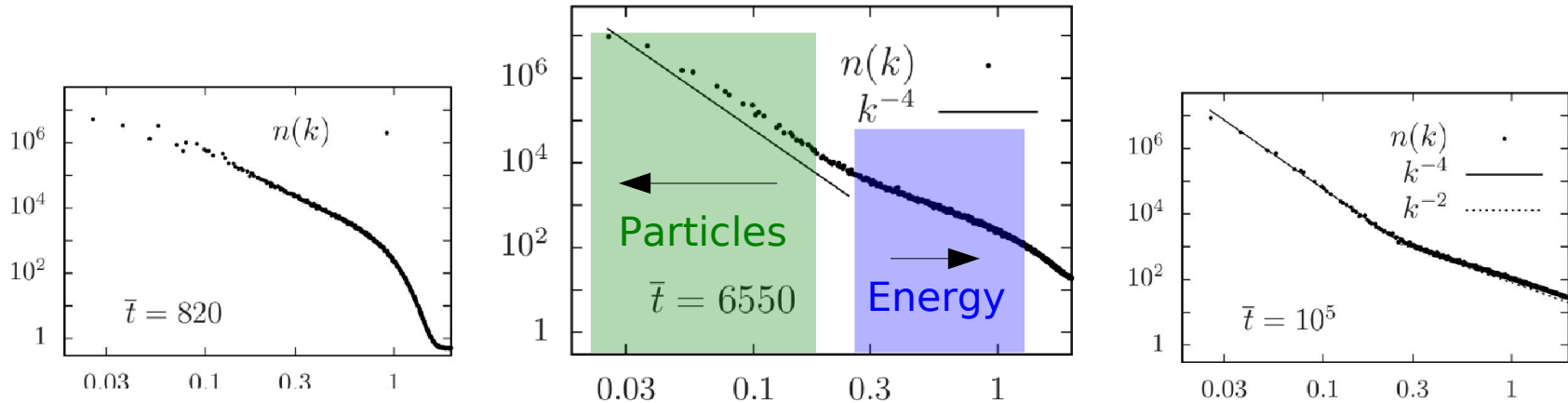
BN, D. Sexty, T. Gasenzer PRB 84(R) (2011), BN, J. Schole, D. Sexty, T. Gasenzer PRA 85 (2012)



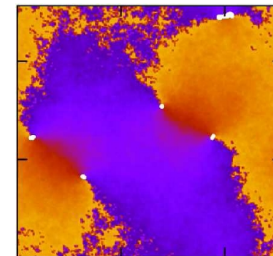
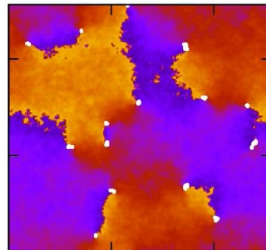
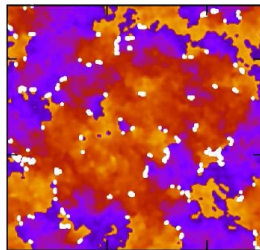
2D: Phase ordering dynamics



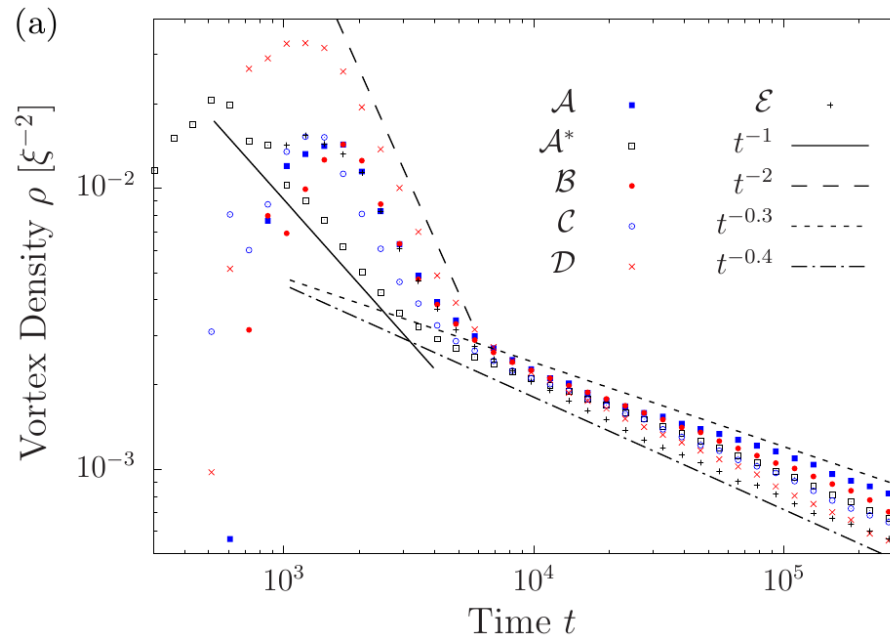
2D: Phase ordering dynamics



Time



2D: Phase ordering dynamics

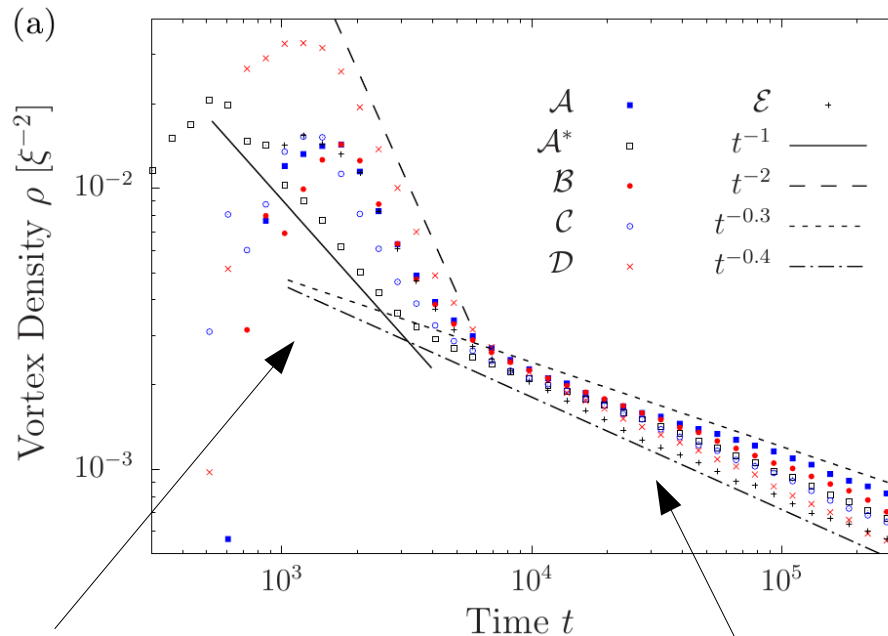


J. Schole, BN, T. Gasenzer, arXiv:1204.2487



2D: Phase ordering dynamics

Scaling needs
vortex unbinding



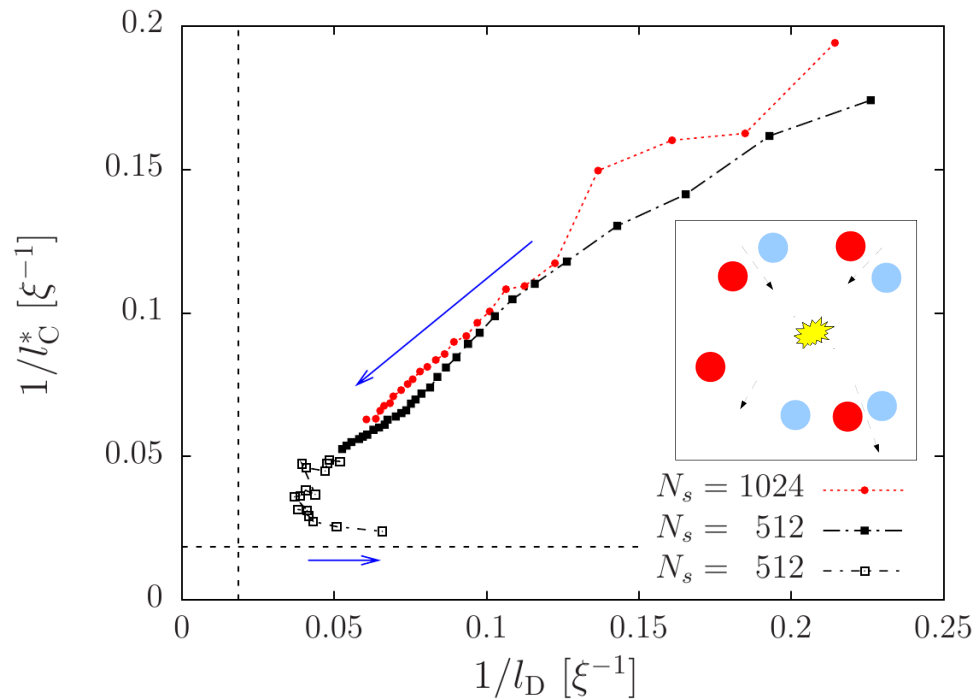
Non-universal decay law
(Initial vortex distribution dependent)
Kinetic gas theory for dipoles

Universal decay regime
Strongly correlated, dilute vortex gas
Scaling $n(k) \sim k^{-4}$

J. Schole, BN, T. Gasenzer, arXiv:1204.2487



Correlations near the NTFP

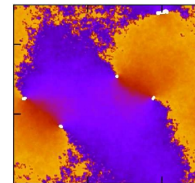
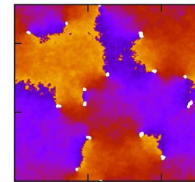
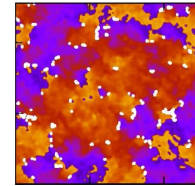
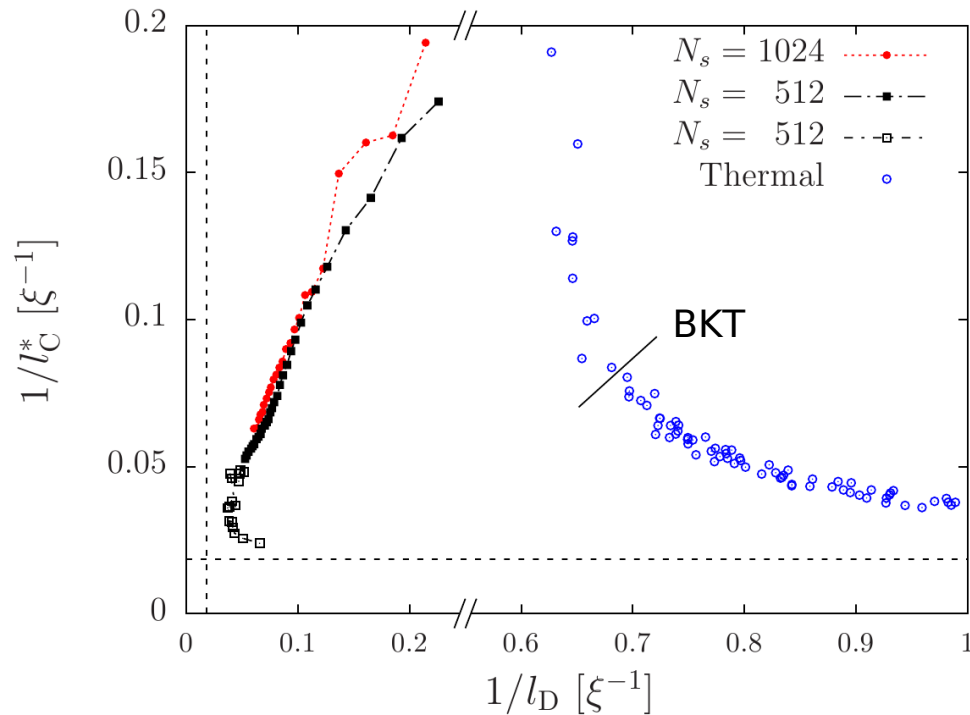


l_C^* Phase coherence length
 l_D Vortex-antivortex pair distance

J. Schole, BN, T. Gasenzer, arXiv:1204.2487



Correlations near the NTFP

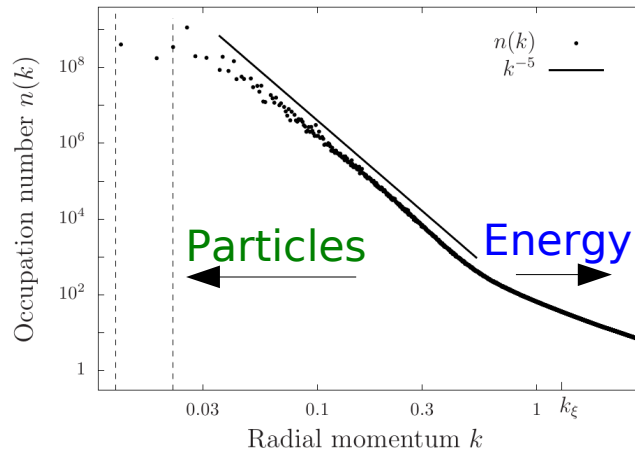
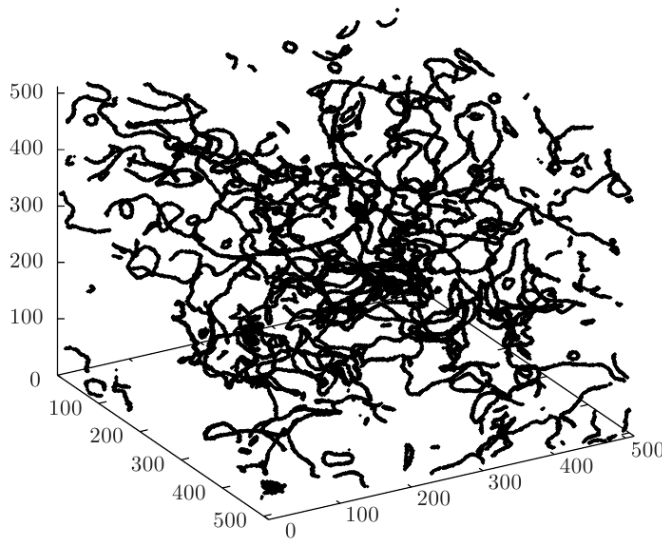


l_C^* Phase coherence length
 l_D Vortex-antivortex pair distance

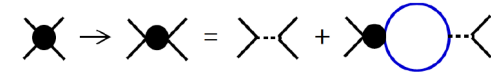
J. Schole, BN, T. Gasenzer, arXiv:1204.2487



3D Nonthermal fixed point

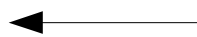


IR: $\zeta = d+2$
 UV: $\zeta = d$

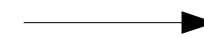


Berges, Rothkopf, Schmidt PRL (2008)
 Scheppach, Berges, Gasenzer PRA (2010)

Vortices



Spectrum $n(k)$



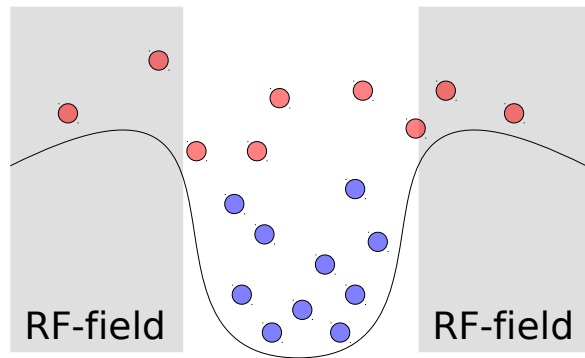
QFT

Condensation dynamics: Kagan, Svistunov, Shlyapnikov ('90s),
 Semikoz, Tkachev (1995), Berloff (2002), Anderson, Davis (2008),
 Blaizot, McLerran(2012), Berges, Sexty (2012)

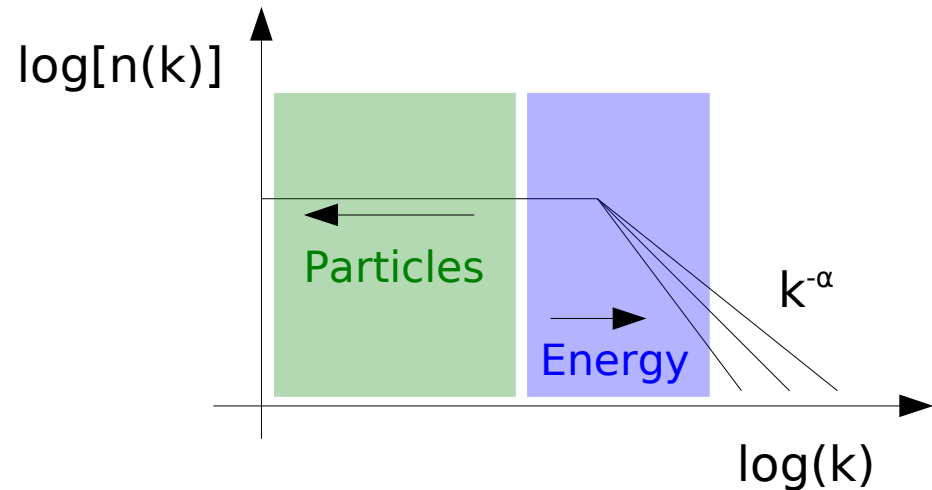
BN, D. Sexty, T. Gasenzer PRB (2011), BN, J. Schole, D. Sexty, T. Gasenzer PRA (2012)



3D: Bose condensation



Evaporative cooling



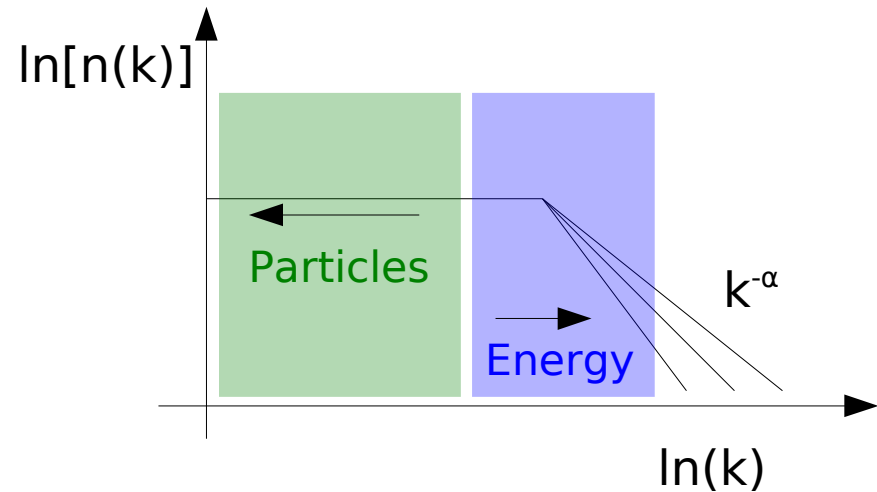
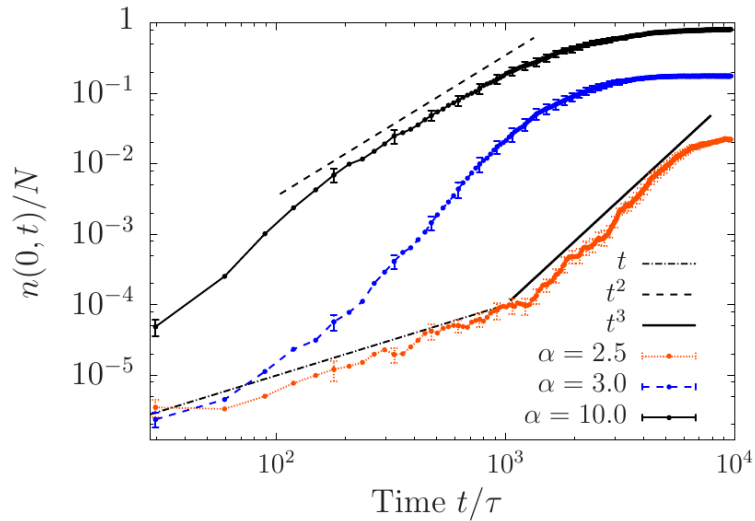
Experiments: Hänsch, Esslinger (2002), Esslinger (2007), Hadzibabic (2012)

Condensation dynamics: Kagan, Svistunov, Shlyapnikov ('90s), Semikoz, Tkachev (1995), Berloff (2002), Anderson, Davis (2008), Blaizot, McLerran (2012), Berges, Sexty (2012)

BN., T. Gasenzer arxiv: 1206.3181



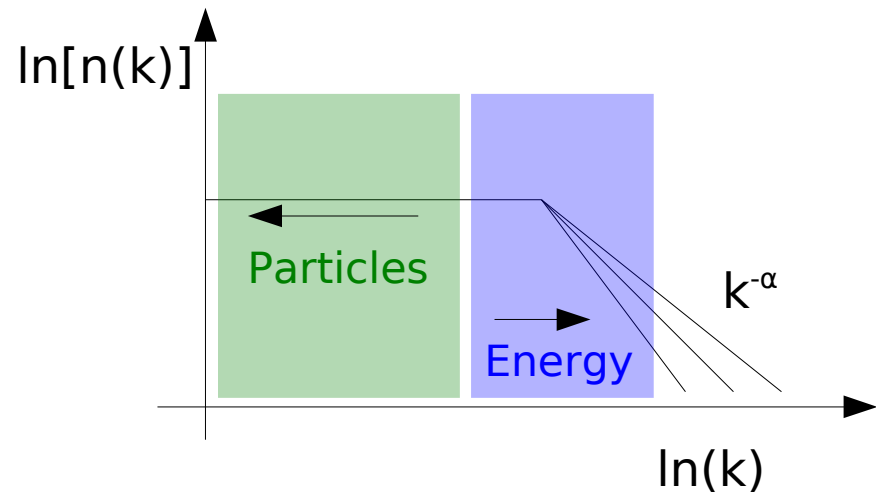
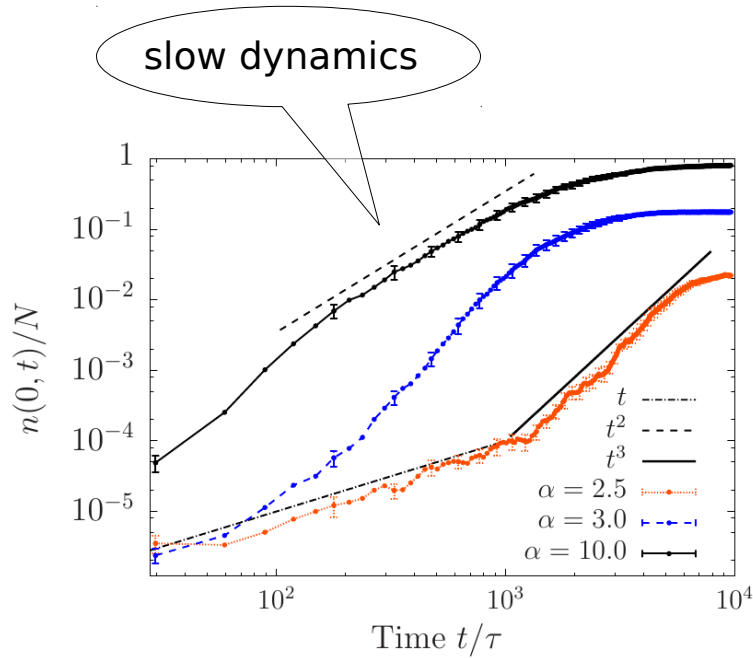
3D: Bose condensation



BN., T. Gasenzer arxiv: 1206.3181



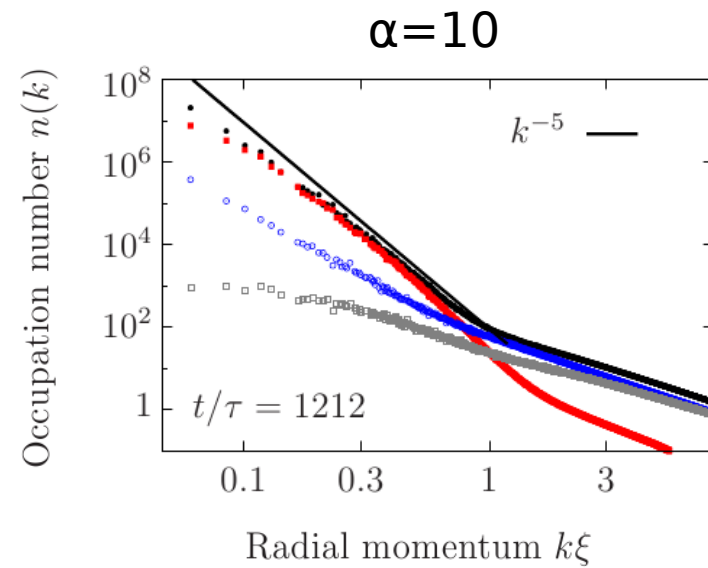
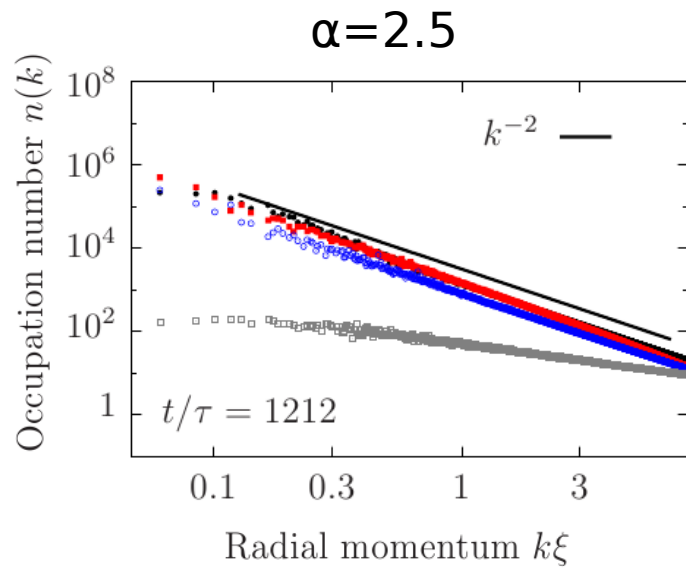
3D: Bose condensation



BN., T. Gasenzer arxiv: 1206.3181



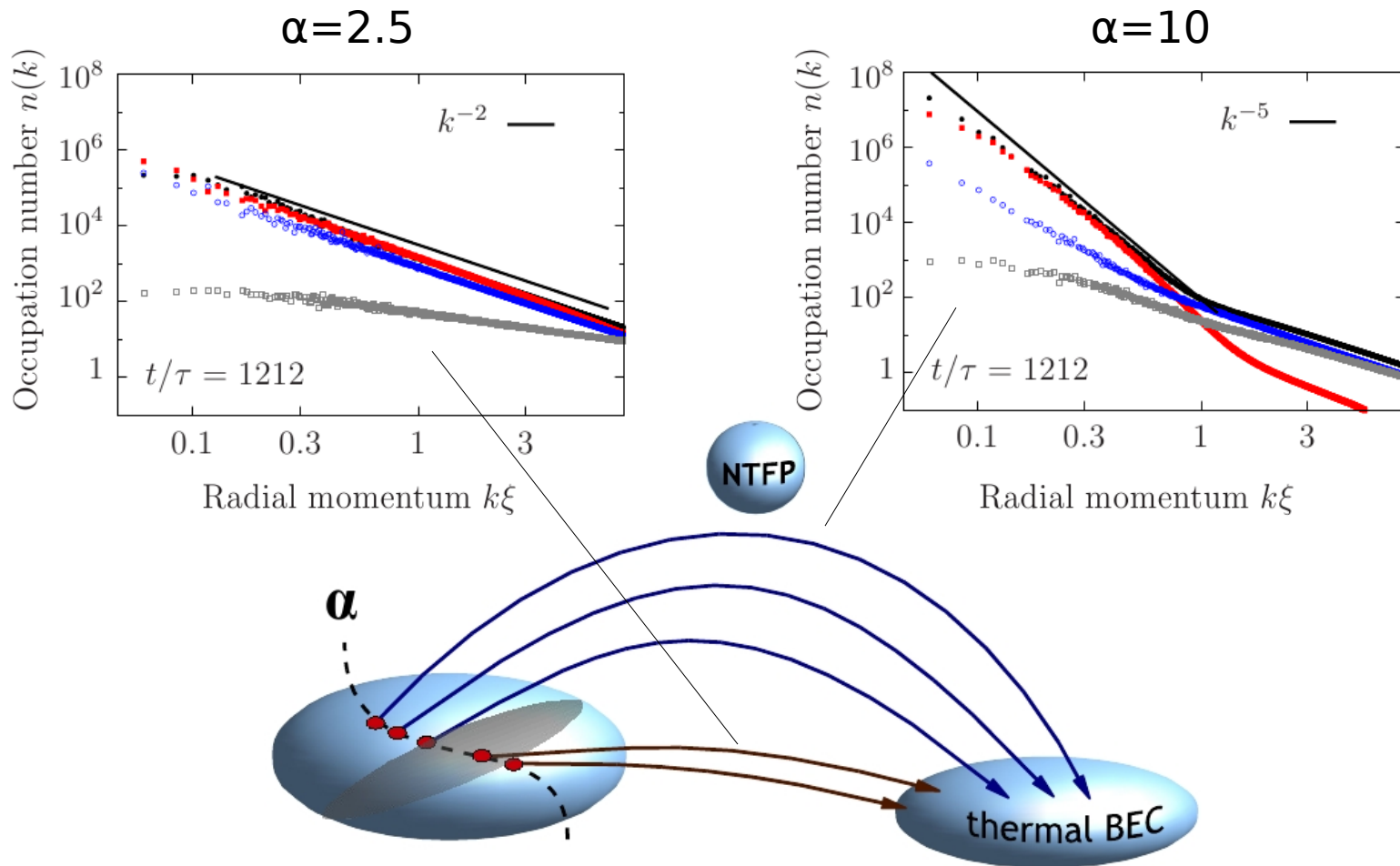
3D: Bose condensation



BN., T. Gasenzer arxiv: 1206.3181



3D: Bose condensation

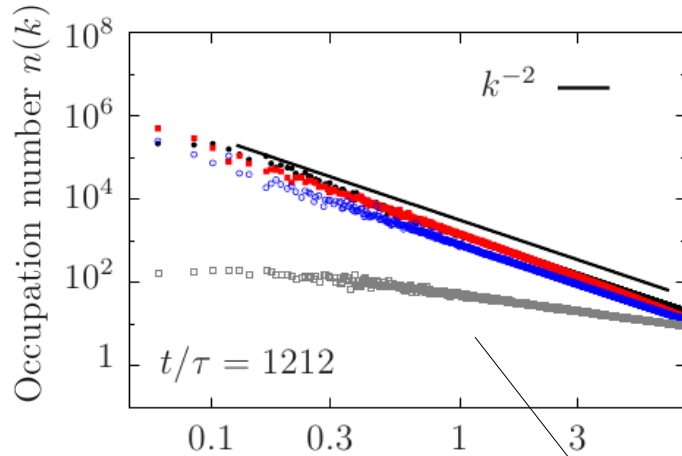


BN., T. Gasenzer arxiv: 1206.3181

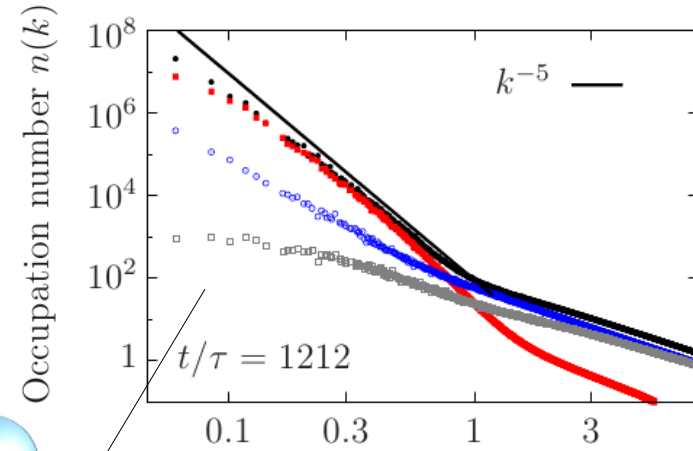


3D: Bose condensation

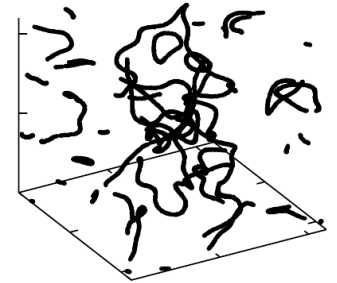
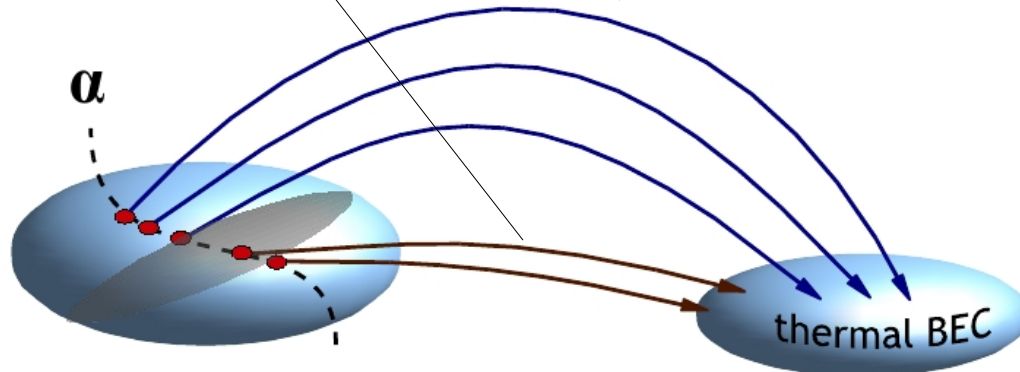
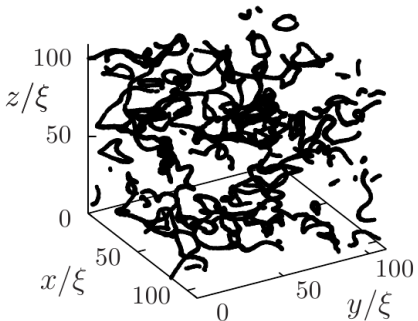
$\alpha=2.5$



$\alpha=10$



NTFP



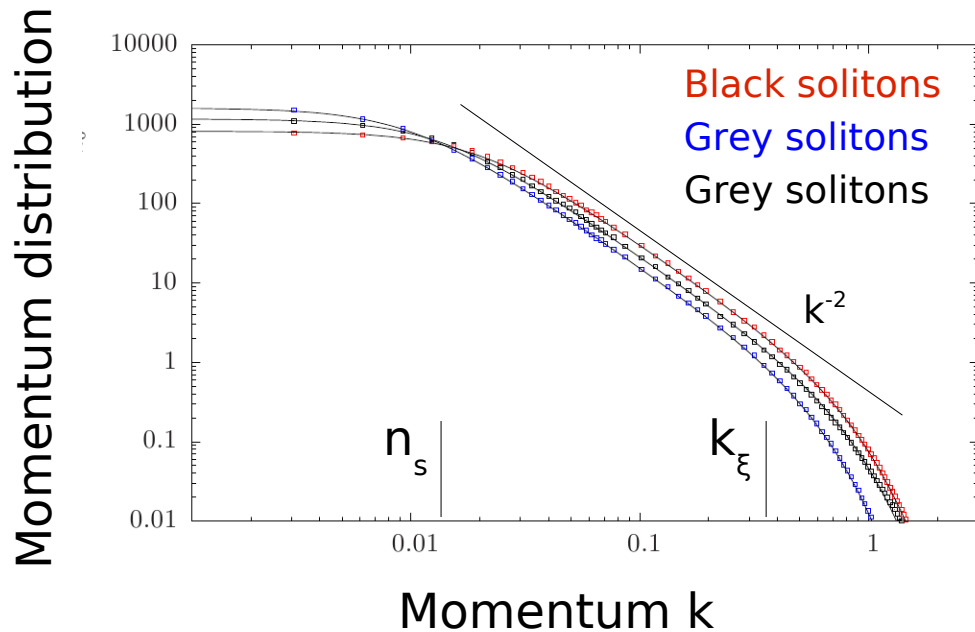
BN., T. Gasenzer arxiv: 1206.3181



1D: Momentum distribution

- Random soliton model for black/grey solitons (in a trap):

e. g.
$$n(k)|_{\nu=0} = \frac{4n_s n}{4n_s^2 + k^2} \frac{(\pi k \xi)^2 / 2}{\sinh^2(\pi k \xi / \sqrt{2})} \quad (\text{Black Solitons})$$

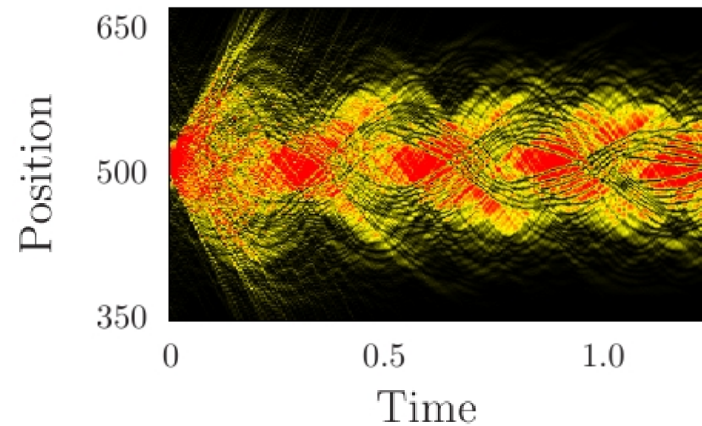
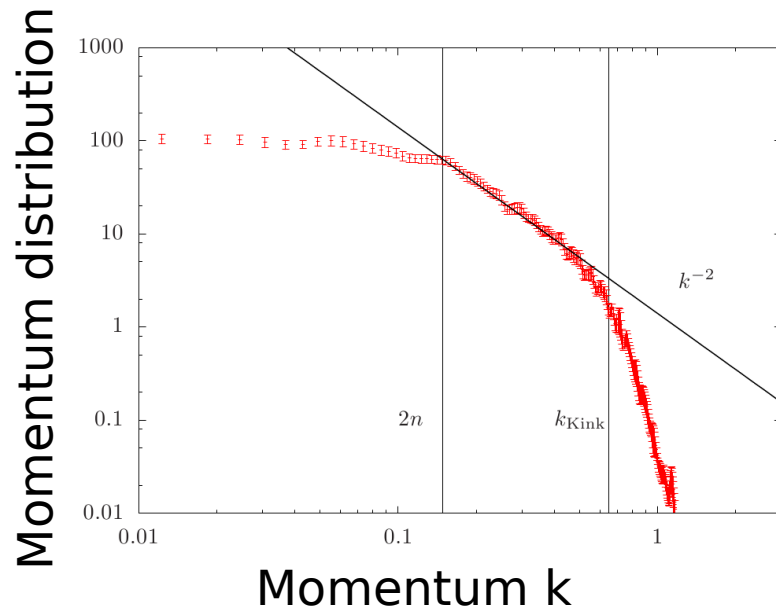


M. Schmidt, S. Erne, BN, D. Sexty, T. Gasenzer NJP (2012), to appear



1D: Quench dynamics

- Features:
- Quasi-stationary profile
 - Scaling



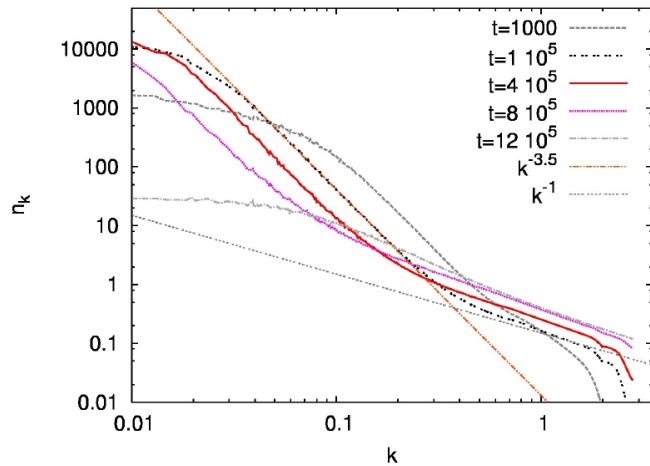
M. Schmidt, S. Erne, BN, D. Sexty, T. Gasenzer NJP (2012), to appear



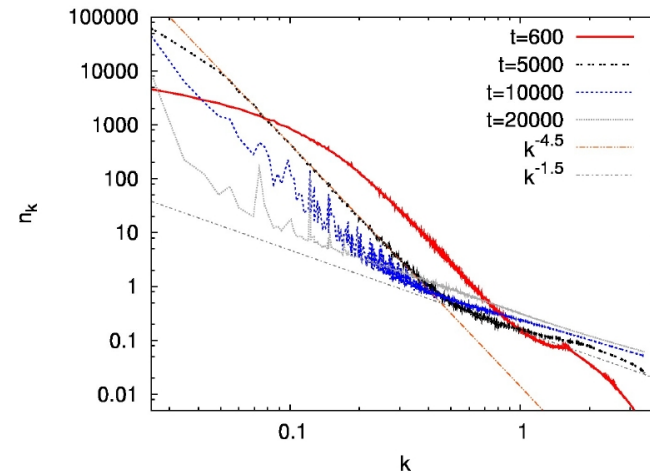
Relativistic simulations

Classical field equation:
$$\left[\partial_t^2 - \Delta + \Phi^2 \right] \Phi_a = 0$$

d=2



d=3



T. Gasenzer, BN, D. Sexty PL (2012)

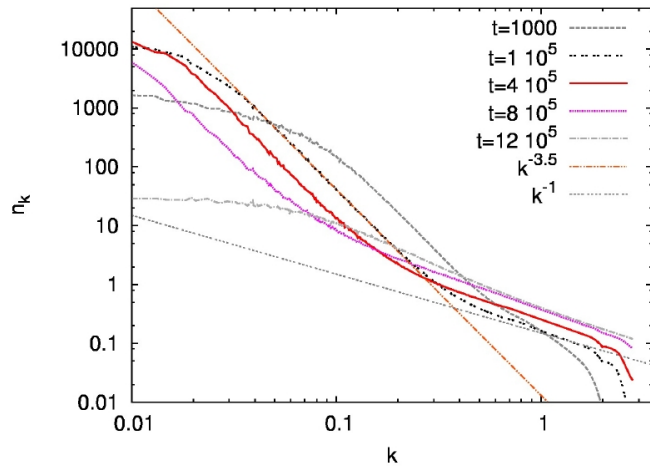
S. Khlebnikov, I. Tkachev PRL (1996)
J. Berges, A. Rothkopf, J. Schmidt PRL(2008)
J. Berges, D. Sexty PRD (2011)



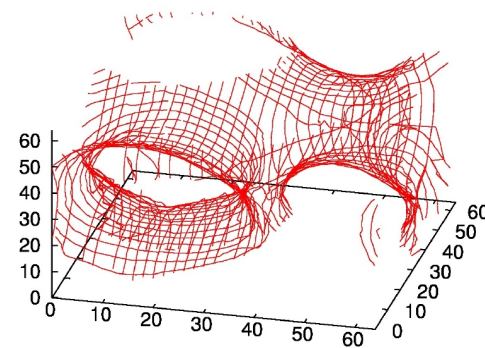
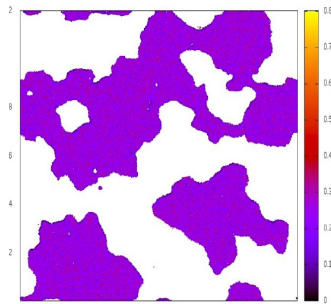
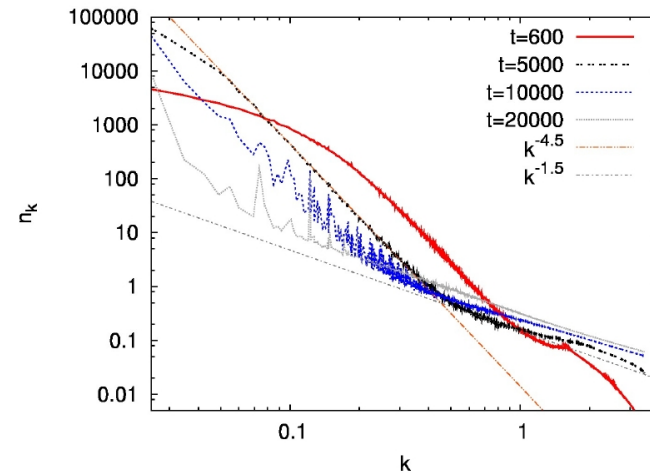
Relativistic simulations

Classical field equation:
$$\left[\partial_t^2 - \Delta + \Phi^2 \right] \Phi_a = 0$$

d=2



d=3



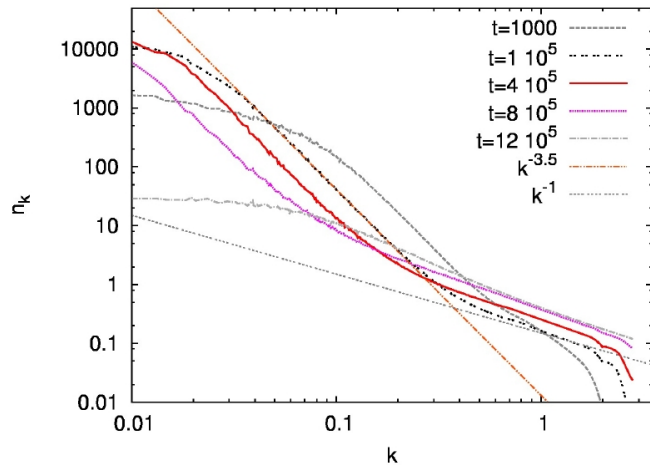
T. Gasenzer, BN, D. Sexty PL (2012)



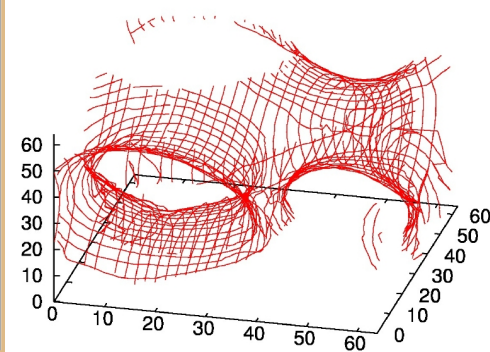
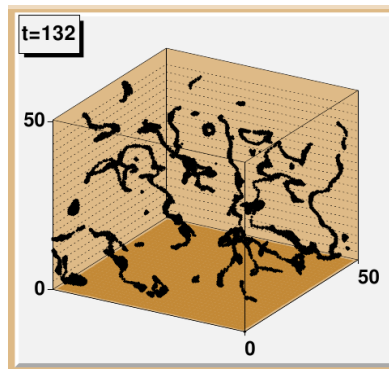
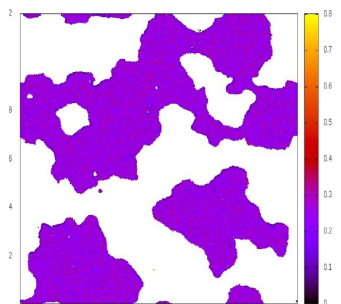
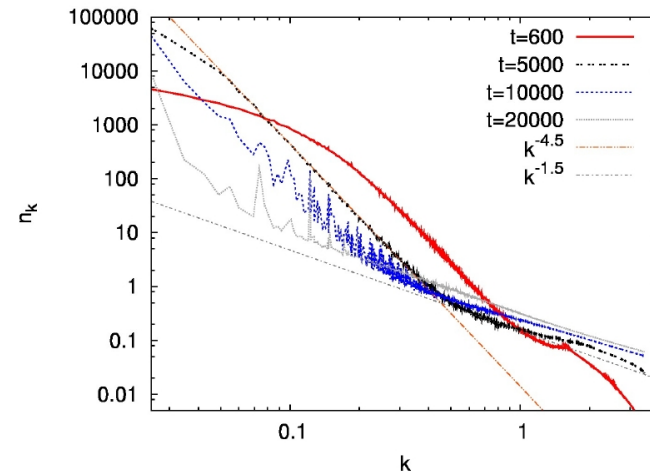
Relativistic simulations

Classical field equation:
$$\left[\partial_t^2 - \Delta + \Phi^2 \right] \Phi_a = 0$$

d=2



d=3



T. Gasenzer, BN, D. Sexty PL (2012) I. Tkachev, S. Khlebnikov, L. Kofman, A. Linde PL (1998)

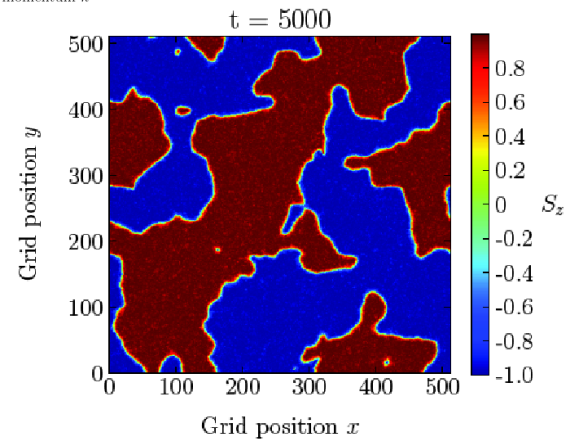
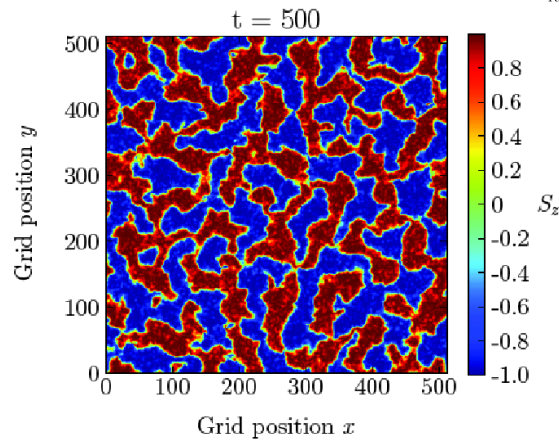
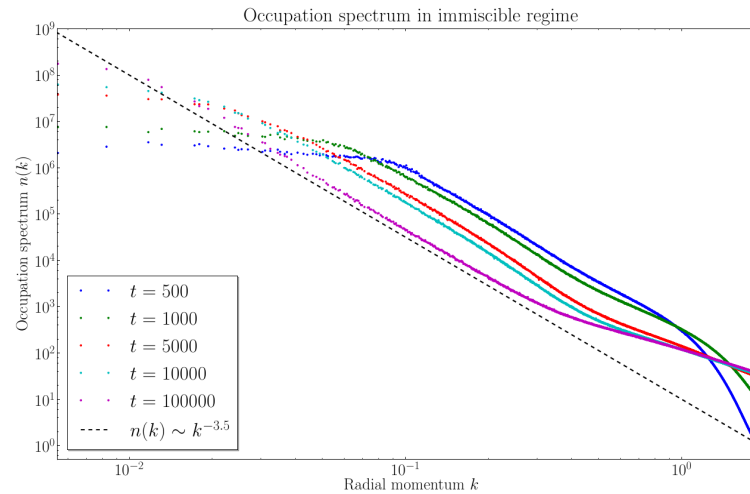


2-component BEC

miscible
 $g_{12} < g$



immiscible
 $g_{12} > g$

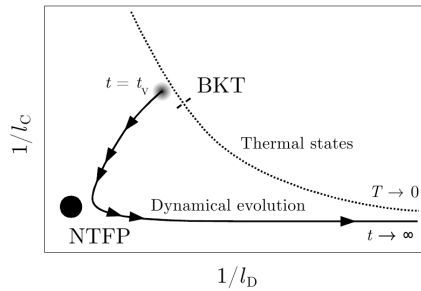
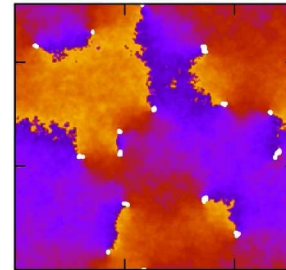


Summary

Nonthermal fixed points (NTFP)

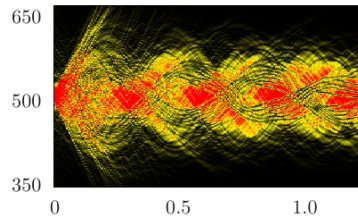
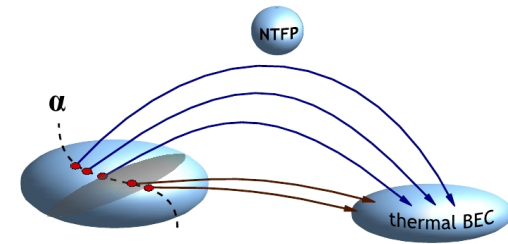


Superfluid turbulence in 2D

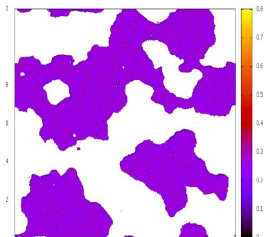


Dynamics near the NTFP in 2D

Dynamic Bose condensation in 3D



Solitonic state as a NTFP



Charge Separation/Domain Walls

